

IEEE Draft P1363.3

Identity Based Public Key Cryptography Based On Pairings

Daniel Schliebner

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Gliederung

Introduction

Identity Based Encryption

BB₁ IBE

The Protocol

Security Of The Protocol

Discussion



About The Headline

Identity Based Public Key Cryptography

- ▶ Is a type of **public-key cryptography**.
- ▶ Difference: the **public-key** is some unique information ID about the **identity** of a user.
- ▶ Proposed by Adi Shamir for the first time in 1984 (see [ASha84] page 47–53).
- ▶ **Paring**: mapping between groups (correct definition later).
- ▶ Used for: **encryption (IBE)**, key encapsulation, signatures (and combinations).



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- ▶ **P1363**: Standardization project for public-key cryptography.
- ▶ **.3**: Specifications for identity-based public-key cryptography using pairings.
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Pairing: a mathematical formalism

Definition

Let $(G_1, +)$, $(G_2, +)$, (G_3, \cdot) be groups of prime order $p \in \mathbb{N}$. A **pairing** is a \mathbb{Z}_p -bilinear map

$$e : G_1 \times G_2 \longrightarrow G_3$$

between \mathbb{Z}_p -modules for which the following holds:

1. e is non-degenerated
(i. e. $\forall P \neq 0_{G_1} \in G_1, Q \neq 0_{G_2} \in G_2 : e(P, Q) \neq 1_{G_3}$).
2. e is computable in an efficient manner.



Now: ID-based cryptography using the example of ID-based encryption.



Identity Based Encryption (IBE)

The Participants

Participants are:

- ▶ **Sender** A (want's to send message m).
- ▶ **Receiver** B (has an identification ID, e. g. bob@domain.com).
- ▶ A Trusted Third Party – the Private Key Generator (**PKG**).



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Identity Based Encryption (IBE)

The Algorithms Of An IBE-Protocol

Algorithms of an IBE-Protocol are:

- ▶ **Setup**: run by the PKG. Returns:
 - ▶ \mathcal{P} – a set of public parameters.
 - ▶ s – the master key (or secret server key).
- ▶ **Extract**(\mathcal{P}, s, ID): run by the PKG (when B requests his private key). Returns:
 - ▶ K_{ID} – the private key corresponding to ID .
- ▶ **Encrypt**(\mathcal{P}, ID, m): run by A . Returns:
 - ▶ c – the encrypted plaintext m .
- ▶ **Decrypt**(\mathcal{P}, ID, c): run by B . Returns:
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Identity Based Encryption (IBE)

The Algorithms Of An IBE-Protocol (cont.)

Summarization:

- ▶ PKG runs **Setup**() $\longrightarrow (\mathcal{P}, s)$.
- ▶ PKG runs **Extract**(\mathcal{P}, s, ID) $\longrightarrow K_{ID}$.
- ▶ A runs **Encrypt**(\mathcal{P}, ID, m) $\longrightarrow c$.
- ▶ B runs **Decrypt**(\mathcal{P}, ID, c) $\longrightarrow m$.



Identity Based Encryption (IBE)

Primitives

- ▶ **Primitives:** contain basic mathematical operations (building blocks for an IBE-protocol).
- ▶ **Generation:** used to extract a private key at a PKG.
- ▶ **Verification:** verification of K_{ID} by receiver B .
- ▶ **Encrypt and Decrypt:** used inside corresponding algorithms.



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- ▶ Security bases on **Bilinear-Diffie-Hellman** (BDH) Problem.
- ▶ As formulated in the previous section, the protocol consists of four algorithms: Setup, Extract, Encrypt and Decrypt.
- ▶ To this end, let G_1, G_2, G_3 be groups of prime order $p \in \mathbb{N}$ and $e : G_1 \times G_2 \rightarrow G_3$ a pairing.
- ▶ Let $ID \in \{0, 1\}^*$ and plaintext $m \in \{0, 1\}^n$.



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BB₁ IBE

Setup

- ▶ PKG chooses a master key

$$s := (s_1, s_2, s_3) \in_R \mathbb{Z}_p^* \times \mathbb{Z}_p^* \times \mathbb{Z}_p^*.$$

- ▶ PKG generates public parameter

$$\mathcal{P} := (Q_1, Q_2, R, T, V, G_1, G_2, e), \text{ where}$$

- ▶ Q_i is a generator of G_i , $i = 1, 2$, i. e. $\langle Q_i \rangle = G_i$,
- ▶ $R := s_1 Q_1$,
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- ▶ $V := e(R, s_2 Q_2)$.



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BB₁ IBE

The primitives (knowing \mathcal{P} and s)

Generation: P-BB1-G(M)

- ▶ $r_0 \in_R \mathbb{Z}_p^*$.
- ▶ $i := s_1 s_2 + r_0 (s_1 M + s_3)$.
- ▶ **return** $(iQ_2, r_0 Q_2)$.

Encryption: P-BB1-E(r)

- ▶ $E_0 := rQ_1$.
- ▶ $E_1 := (rM)R + rT$.
- ▶ $B := V^r$.
- ▶ **return** (E_0, E_1, B) .

Decryption: P-BB1-D($E_0, E_1, (K_{0,M}, K_{1,M})$)

- ▶ **return** $e(E_0, K_{0,M}) \cdot e(E_1, K_{1,M})^{-1}$.



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- ▶ There are three algorithms left.
- ▶ Using the three primitives P-BB1-G, P-BB1-E, P-BB1-D we can now formulate them.
- ▶ Therefore: consider three Hashfunctions

$$\begin{array}{lcl}
 H_1 : & \{0, 1\}^* & \longrightarrow \mathbb{Z}_p^* \\
 H_2 : & G_3 & \longrightarrow \{0, 1\}^n \\
 H_3 : & G_3 \times \{0, 1\}^n \times G_1 \times G_1 & \longrightarrow \mathbb{Z}_p^*
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Extract

- ▶ $M := H_1(\text{ID})$.
- ▶ $K_{\text{ID}} := (K_{0,M}, K_{1,M}) \leftarrow \text{P-BB1-G}(M)$.

K_{ID} is the private key for the receiver.



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Encrypt

- ▶ $r \in_R \mathbb{Z}_p^*$.
- ▶ $(B, E_0, E_1) \leftarrow \text{P-BB1-E}(r)$.
- ▶ $Y := H_2(B) \oplus m$.
- ▶ $t := r + H_3(B, Y, E_0, E_1)$.
- ▶ $c := (Y, E_0, E_1, t)$.

c is the ciphertext. B is called **blinding factor**.



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- ▶ $B \leftarrow \text{P-BB1-D}(E_0, E_1, K_{\text{ID}})$.
- ▶ $r := t - H_3(B, Y, E_0, E_1)$.
- ▶ **if** $\neg(B == V^r$ **and** $E_0 == rQ_1)$ **then exit with** „error“.
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Security

Definition

Let $e : G_1 \times G_2 \longrightarrow G_3$ be a pairing and $P \in G_1, Q \in G_2$. The **Bilinear-Diffie-Hellman** (BDH) Assumption says, that if P, Q, aP, bP, aQ, cQ for $a, b, c \in \mathbb{Z}_p^*$ are given, then it is hard to compute $e(P, Q)^{abc}$.



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Security (cont.)

The security depends on

- ▶ Hashfunctions H_1, H_2, H_3 .
- ▶ The secure channel between the receiver and the PKG.
- ▶ The BDH Assumption (at which point?).



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Security (cont.)

Definition

Let $q \in \mathbb{Z}_p^*$. Then the q -**Bilinear-Diffie-Hellman-Inverse** (q -BDHI) Assumption says, that if $(P, aP, a^2P, \dots, a^qP, Q, aQ, \dots, a^qQ)$ are given, it is hard to compute $(e(P, Q)^a)^{-1}$.

Definition

We say, that the (t, q, ε) -BDHI Assumption holds, if no t -time algorithm \mathcal{A} has advantage ε (i. e.

$P(\mathcal{A}(P, \dots, a^qP, Q, \dots, a^qQ)) \geq \varepsilon$) in solving the q -BDHI problem.



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Security (cont.)

Definition

We say, that an IBE system is **(t, q_{ID}, ϵ) -selective identity, chosen plaintext secure** (short: (t, q_{ID}, ϵ) -IND-sID-CPA secure) iff for every IND-sID-CPA adversary \mathcal{A} , that makes at most q_{ID} chosen private key queries, there is $ADV_{\mathcal{A}} < \epsilon$, where $ADV_{\mathcal{A}}$ is the advantage of \mathcal{A} , attacking the IBE system.



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Security (cont.)

Theorem

Suppose the (t, q, ε) -BDHI Assumption holds for G_1 and G_2 . Then BB₁ IBE is (t', q_S, ε) -IND-sID-CPA secure for any $q_S < q$ and any $t' < t - \Theta(\tau q^2)$, where τ is the maximum time for an exponentiation in G_1, G_2 .

Proof: see [BB04].



Advantages



Advantages

- ▶ IBE eliminates the need for a public key distribution infrastructure.
- ▶ No key agreement.
- ▶ Interesting features (e. g. encode additional information into the ID: for instance expirations dates).



Disadvantages



Disadvantages


- ▶ PKG may decrypt and/or sign any message without authorisation.
- ▶ A secure channel is required between the PKG and the receiver.




That's it. Thank you for your attention.



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